



Research Article

Finite Element Analysis of an Aircraft Morphing Wing

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| Keywords | Abstract |
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| Morphing wing, Aircraft, Finite Element Analysis, Wings Design. | Aircraft wings are a compromise that allows the aircraft to fly at a range of flight conditions. Wings of the morphing type are meaningful advancements of the conventional structures as they are benefit to maneuverability and economy of aircrafts. Aims to demonstrate features of morphing wings' performance, this paper conducts a comprehensive Finite Element Analysis to a morphing wing after the object had been carefully designed. The deformation, strain energy, equivalent stress, and equivalent elastic strain of the morphing wing after applying a certain pressure are reached according to the constructed Finite Element model. Conclusion such as stress concentration point, maximum deformation, etc. of the morphing wing are suggested according to the analytic results. |

1. Introduction

Air planes have played an important role in history since the first airplane was invented in 1903 [1, 2]. Developments in science and technology have led to more advanced air plane structures that offer high efficiency, lower cost, greater maneuver ability, the ability to cruise, and so forth [3, 4]. In recent years, the study of airplane wings has become a hot topic, with the particular interest in morphing wings [3-6]. Originally, morphing wings are inspired by birds, which have a large potential to improve the overall aircraft performances [7, 8]. Morphing aircraft are multi-role aircraft that change their external shape substantially to adapt to a changing mission environment during flight [8]. This creates superior system capabilities not possible without morphing shape changes. The objective of morphing activities is to develop high performance aircraft with wings designed to change shape and performance substantially during flight to create multiple-regime, aerodynamically-efficient, shape-changing aircraft [8-10]. Compared to conventional aircraft, morphing aircraft become more competitive as more mission tasks or roles are added to their requirements.

Morphing wing has been in aviation industry. Firstly, Wright brothers decided to use twist which is out of plane type of morphing wing, they used it to roll the aircraft and it worked [8, 11]. As years pass by many aeronautical

engineers started getting interested in morphing wing concept and started to experiment, the problem they were facing was with the material which can be used efficiently and at low cost [8, 12]. In 1951 the aircraft X-5 was flown with variable sweep wing which could change its shape depending on speed and it was quite efficient and later on aircrafts such F14 and F111 were also using same design geometry and this time the material was using Titanium which was very strong and light material, it is being used still in aviation industry [13, 14]. Designers faced the problem of weight which still continues to be the problem for morphing wing aircraft but they did not let this issue to stop them so many designers designed morphing wing technology and applied into smaller scale in aircraft which included chord changing, leading and trailing edge changing, flaps changing one of the examples were F16 and F18 which uses leading edge changing morphing technology which is quite beneficial [14]. Latest and very successful example of morphing wing technology is Morphing Flap system which was made by Flexsys company for the Gulf Learjet [15-17]. Designers are continuing to find appropriate design of morphing wing which will be efficient in fuel, would be having less weight and at the same time less cost price [8, 17].

The current use of multiple aerodynamic devices (such as flaps and slats) represents a simplification of the general idea

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behind morphing. Traditional control systems (with fixed geometry and/or location) give high aerodynamic performance over a fixed range and for a limited set of flight conditions [17, 18]. Outside of this range, these traditional systems can be neutral or negatively influence the aerodynamics and hence often give lower efficiency [17, 19]. Conventional hinged mechanisms are effective in controlling the airflow, but they are not efficient, as the hinges and other junctions usually create discontinuities in the surface, resulting in unwanted fluid dynamic phenomena. Since 1920, airplanes have used devices that can increase the lift during landing and takeoff [20]. Increases in aircraft weight, cruise speed, and increases in the wing structural stiffness to avoid multiple aero-elastic phenomena (divergence, flutter, etc.) have led to the use of discrete control surfaces such as ailerons and flaps in place of wing twist [8, 17]. Researchers, gradually, seriously revisited concepts of variable wing shape. Most of this research was based on two concepts, namely the active control of the curvature along the wingspan and the implementation of flexible wings, able to exploit the aero-elastic forces to obtain the desired deformations (wing shapes) [21, 22].

Civilian airplanes consume large amounts of fuel during a flight [23, 24]. The weight of fuel accounts for more than 30% of the airplane's total weight [17, 24]. A morphing wing with a variable camber trailing edge reduces fuel consumption by at least 5% and increases the lift coefficient from 0.08 to 0.4 [8, 17, 23, 24].

Changing the wing shape or geometry is not new. Historically, morphing solutions always led to penalties in terms of cost, complexity, or weight, although in certain circumstances, these were overcome by system-level benefits [25]. The current trend for highly efficient and 'green' aircraft makes such compromises less acceptable, calling for innovative morphing designs able to provide more benefits and fewer drawbacks [26]. Recent developments in 'smart' materials may overcome the limitations and enhance the benefits from existing design solutions. The challenge is to design a structure that is capable of withstanding the prescribed loads, but is also able to change its shape.

Under the condition that the performance of morphing wings of aircraft is limited, this paper presents a detailed feature analysis of a designed morphing wing by using Finite Element Analysis (FEA) to demonstrate the corresponding mechanical properties of the morphing wing. The remainder of this paper is arranged as follows. Section 2 presents some basic concepts associated with morphing wings. Section 3 introduced the morphing wing model of this study. The FEA is implemented in Section 4. Conclusion of this study is provided in Section 5.

2. Basic Concepts of Morphing Wing

2.1. Wing Profile

A typical wing profile is displayed in Figure 1. In aeronautics, the thickness ratio compares the maximum vertical thickness of a wing to its chord. It is a key measure of the performance of a wing planform when it is operating at transonic speeds. To be specific, in civil aircraft, it is possible to come across wing profiles with various thickness

ratios between 8-9% and 18-20% depending on the duty speed of the plane. Typically, thickness ratio of wing profile can be divided into thin profile (thickness ratio less than 0.1), medium thickness profile (0.1-0.14), and thick profile (over 0.14) [27].

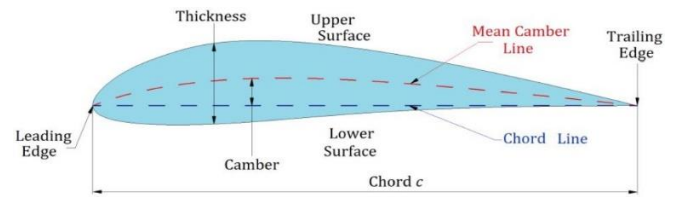


Figure 1. Typical wing profile geometry

The maximum thickness point is usually between 30% and 60% of the vet. In some old profiles it is possible to see that this point is at 25% of the vet. In some exceptional profiles, the maximum thickness point can be found lower than 60% of the veterinarian. Wing profiles can be symmetrical or humped. Symmetrical profiles are not used in aircraft wings, rather, they are used on vertical and horizontal tail surfaces, in the connecting elements between the wings of biplane aircraft, in the bodywork of the elements that create parasitic resistance on the aircraft such as landing gear and so on. To be comparable, humpbacks between 0 and 5% are found on the airplane wings. It is possible to see more humped profiles in turbines and compressors.

Overall, 2 force components (Carriage and Drag) and 1 moment component (Pitching) affect the wing profile. It is possible to achieve transport and drag by integrating the pressure distribution across the surface. Although it seems possible to find drag by integrating pressure and friction distributions across the surface, this is generally very difficult. Therefore, drag is obtained by measuring the loss of momentum. Although the performance of the wing profile determines the Transport and Drag forces and the Pitching moment, it is often concerned with these coefficients instead of these force and moment components. In general, the aerodynamic coefficients of the wing profile depend primarily on the geometric shape and angle of attack of the profile, and then on the Reynolds and Mach numbers.

2.2. Angle of Attack

In fluid dynamics, angle of attack is the angle between a reference line on a body (often the chord line of an airfoil) and the vector representing the relative motion between the body and the fluid through which it is moving [28]. Angle of attack is the angle between the body's reference line and the oncoming flow. This article focuses on the most common application, the angle of attack of a wing or airfoil moving through air.

In aerodynamics, angle of attack specifies the angle between the chord line of the wing of a fixed-wing aircraft and the vector representing the relative motion between the aircraft and the atmosphere. Since a wing can have twist, a chord line of the whole wing may not be definable, so an alternate reference line is simply defined. Often, the chord line of the root of the wing is chosen as the reference line. Another choice is to use a horizontal line on the fuselage as the reference line (also as the longitudinal axis).

Low angle of attack results in sufficient buoyancy, while an over-high angle of attack causes turbulence and may even cause the blade to break in the air stream. Therefore, designers must ensure that the angle of attack is at optimal levels (15 degrees generally).

The critical angle of attack is the angle of attack which produces the maximum lift coefficient. This is also called the "stall angle of attack". Below the critical angle of attack, as the angle of attack decreases, the lift coefficient decreases. Conversely, above the critical angle of attack, as the angle of attack increases, the air begins to flow less smoothly over the upper surface of the airfoil and begins to separate from the upper surface. On most airfoil shapes, as the angle of attack increases, the upper surface separation point of the flow moves from the trailing edge towards the leading edge. At the critical angle of attack, upper surface flow is more separated and the airfoil or wing is producing its maximum lift coefficient. As the angle of attack increases further, the upper surface flow becomes more fully separated and the lift coefficient reduces further.

Above this critical angle of attack, the aircraft is said to be in a stall. A fixed-wing aircraft is stalled at or above the critical angle of attack rather than at or below a particular airspeed. The airspeed at which the aircraft stalls varies with the weight of the aircraft, the load factor, the center of gravity of the aircraft and other factors. However, the aircraft always stalls at the same critical angle of attack. The critical or stalling angle of attack is typically around 15-20 degrees for many airfoils.

3. Morphing Wing Design

The design of the morphing wing follows the predetermined steps [29-31]:

(1) Model determination. The NASA sc(2)-0714 model was selected to be the aircraft model of this study (two Dimensional (2D) coordinates of which is available at <http://airfoiltools.com/>), see Figure 2.

(2) Extend 2D coordinates to 3D view. Transfer the 2D coordinates to Microsoft EXCEL and then add the z coordinates as zero to obtain the 3D view.

(3) 3D model establishments. Save values in Step (2) text form to transfer SOLIDWORKS software and configure the 3D model of the morphing wing.

The morphing wing is divided into two different parts: fixed part (part 1) and morphing part (part 2).

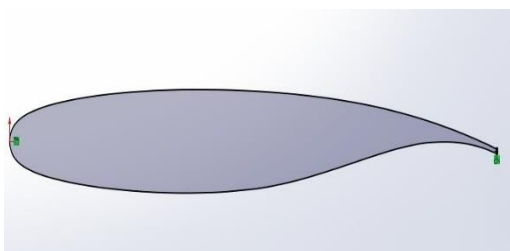


Figure 2. 2-D View of the wing

4. Finite Element Analysis (FEA)

To create buoyancy, the surface area of the upper part of the morphing wing is larger than the lower side. Due to this difference, a high-pressure area occurs in the lower section and a low-pressure area in the upper section. Thanks to this

pressure difference, the buoyancy can be obtained from the air.

To observe the mechanical reaction of the morphing wing against this pressure difference, we create a high-pressure area at the bottom of the morphing wing and apply it to the wing through the ANSYS program. The aim in doing this is to observe the stress, resistance, and deformation changes that may occur on the wing and to determine the critical points on the morphing wing model.

The analytic steps using ANSYS for analysis of the morphing wing as follows [32-36]:

(1) Save and then transfer the morphing wing model from SOLIDWORKS to ANSYS.

(2) Parameter definition. Define geometry, material (Aluminum), etc. of the morphing wing in the finite element model in the ANSYS software.

(3) Meshing: Mesh, elaborately, the finite element model in the ANSYS software.

(4) Analysis implementation. Conduct analysis and monitor outcomes as deformation, stress, strain, and energy change.

The deformation, strain energy, equivalent stress, and equivalent elastic strain of the morphing wing after applying 1 MPa pressure is displayed in Figures 3-6, respectively.

As seen from the Figure 3, after applying pressure, maximum deformation occurs at the end points of our wing. Since these parts are the most distant parts of our wing from the main body, as a result of the strength calculations, the most force occurs in the extreme regions. Therefore, deformation in the extreme regions is more. In contrast, as the surface area, the least amount of expansion occurs in the parts of the wing welded to the main body. The reason for this is that the momentum acting on those regions is less. Therefore, minimum deformation occurs in areas close to the body.

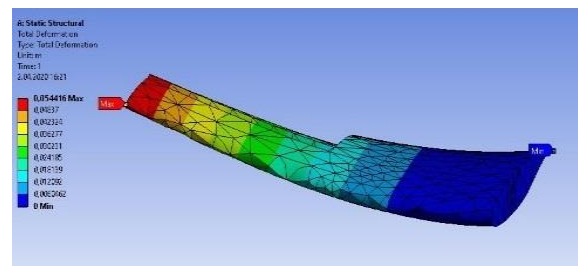


Figure 3. Deformation of morphing wing after 1 MPa pressure applied

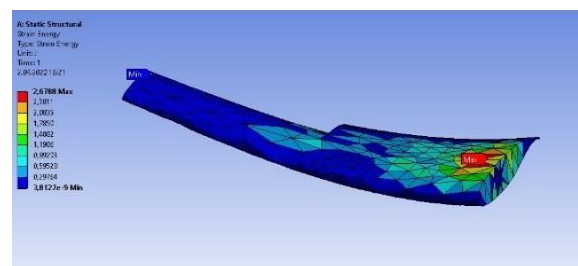


Figure 4. Strain energy distribution of the morphing wing after 1 MPa pressure applied

The total shear energy changes occur mostly in the upper part of the morphing wing, closest to the body. The slip occurs perpendicular to the lateral axis. And it tends to

happen in fixed sections with the most reaction force. Since less energy is dissipated to the tip of the morphing wing, less compensating force is generated at the tip. And this results in less strain energy occur at the ends.

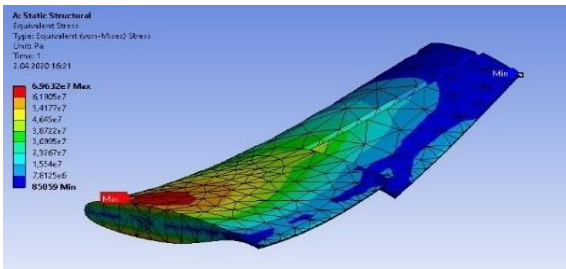


Figure 5. Equivalent stress distribution of the morphing wing after 1 MPa pressure applied

As shown in the Figure 5, the maximum equivalent stress occurs in the parts of the upper part of the wing closest to the main body. The pressure acting from below causes the wing to bend upwards. And this causes the wing to squeeze the upper parts and the lower parts to elongate. For this reason, the maximum equivalent stress occurs in these regions. Since the opposite is true at the ends, the minimum equivalent stresses are obtained at the ends as shown in the Figure 5.

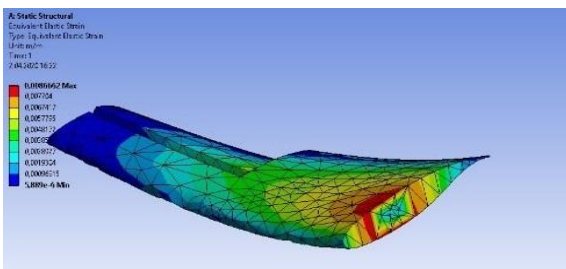


Figure 6. Equivalent elastic strain of the morphing wing after 1 MPa pressure applied

As shown in the Figure 6, the maximum equivalent elastic strain is seen in the center and near the part of the wing closest to the main body. Since the morphing wing is welded to the main body, the maximum elastic strain tendency is observed in the center and the periphery of the wing close to the body. However, since the ends of the morphing wing are far from the welded part, the amount of energy to be generated in those parts is minimum. Therefore, equivalent elastic slip occurs in the minimum amount in the end parts of the plane where it can be seen from the shape.

As can be seen from all these analyzes, different regions of the wing gave various reactions to different types of analysis. And basically, it is concluded that the critical points are the tip of our wing and the part welded to the body. Because energy and deformation changes took place in these regions with maximum and minimum. These analyzes are very important. Because the evaluation and scoring of any product designed is done by looking at these analyzes. And if necessary, the design can be redone in some projects. As a result, these analyzes are very important results that shed light on us.

5. Conclusions

Wings of the morphing type are meaningful advancements of the conventional structures as they are benefit to maneuverability and economy of aircrafts. This paper conducts a comprehensive Finite Element Analysis to a morphing wing after the object had been carefully designed. The following conclusions are achieved based on the outcomes of the analysis:

(1) Maximum deformation occurs at the end points of the morphing wing as these parts are the most distant parts from the main body. The expansion of the parts of the wing welded to the main body is minor.

(2) The total shear energy changes occur mostly in the upper part of the morphing wing, closest to the body.

(3) The maximum equivalent stress occurs in the parts of the upper part of the wing closest to the main body.

(4) The maximum equivalent elastic strain is in the center of the wing and at the meanwhile the equivalent elastic slip occurs in the minimum amount in the end parts of the plane. As a direction for future work we will consider applying some techniques such as but not limited to [36-51].

Conflict of Interest Statement

The authors declare no conflict of interest.

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